

# Derivation of Bond Demand Curve - Example

To derive the demand for bonds, suppose that we have:

- discount bond (no coupon payments)
- maturity = 1 year
- face value = \$1,000
- holding period = maturity = 1 year (hence the expected return is equal to the "interest rate", i.e. the yield to maturity)

Next, we will assume different prices and corresponding quantities demanded (and calculate the interest rates)

Derivation of Bond Demand Curve – Example (cont.)

Remember that, in this case,

$$i = R = \frac{F - P}{P}$$

- Point A:
  - P = \$950
  - $B^d$  = \$100 billion
  - $i = \frac{\$1,000 \$950}{\$950} = 5.3\%$

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### Derivation of Bond Demand Curve -Example (cont.)

- Point B:
  - P = \$900
  - $B^d$  = \$200 billion

$$i = \frac{\$1,000 - \$900}{\$900} = 11.1\%$$

- Point C: P = \$850,  $B^d = \$300$  billion, i = 17.6%
- Point D: P = \$800,  $B^d = \$400$  billion, i = 25.0%
- Point E: P = \$750,  $B^d = \$500$  billion, i = 33.0%
- Demand curve  $B^d$  connects points A, B, C, D, E and has the usual downward slope

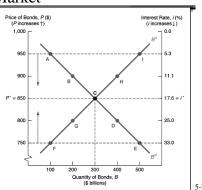
Derivation of Bond Supply Curve – Example (cont.)

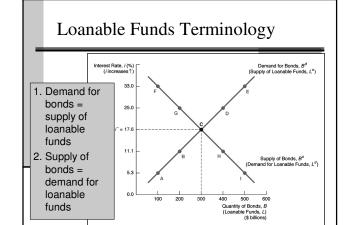
- Point F: P = \$750, i = 33.0%,  $B^s = $100$  billion
- Point G: P = \$800, i = 25.0%,  $B^s = \$200$  billion
- Point C: P = \$850, i = 17.6%,  $B^s = \$300$  billion
- Point H: P = \$900, i = 11.1%,  $B^s = $400$  billion
- Point I: P = \$950, i = 5.3%,  $B^s = \$500$  billion
- Supply curve B<sup>s</sup> connects points F, G, C, H, I, and has an upward slope

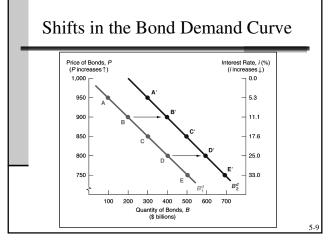
## Supply and Demand Analysis of the Bond Market

### Market Equilibrium 1. Occurs when

- $B^d = B^s$ , at  $P^* = $850$ , i\* = 17.6%
- 2. When P = \$950,  $i = 5.3\%, B^s > B^d$ (excess supply):  $P \downarrow$ to  $P^*$ ,  $i \uparrow$  to  $i^*$
- 3. When P = \$750,  $i = 33.0, B^d > B^s$ (excess demand):  $P \uparrow$  to  $P^*$ ,  $i \downarrow$  to  $i^*$







### Shifting versus Moving along a Line

- Need to distinguish between two kinds of changes:
  - movement along a curve: e.g., if the price changes, the quantity demanded changes, so there is a movement along the demand curve
  - shift in a curve: e.g., people have a sudden interest in the bond market, which increases the demand for bonds at any given price

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# Factors that Shift the Bond Demand Curve

#### ■ Wealth

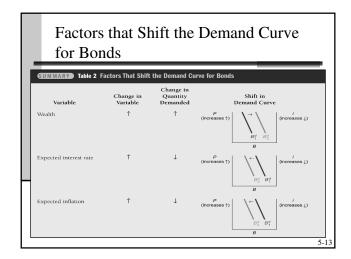
- boom or more savings, wealth  $\uparrow$ ,  $B^d \uparrow$ ,  $B^d$  shifts out to right
- Expected return
  - $i \lor i$  in the future, R for long-term bonds  $\uparrow$ ,  $B^d$  shifts out to right
  - $\pi^e \Psi$ , relative return  $\uparrow$ ,  $B^d$  shifts out to right
  - expected return of other assets  $\Psi$ ,  $B^d \uparrow$ ,  $B^d$  shifts out to right

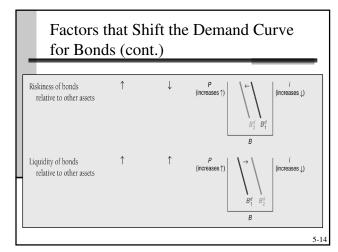
# Factors that Shift the Bond Demand Curve (cont.)

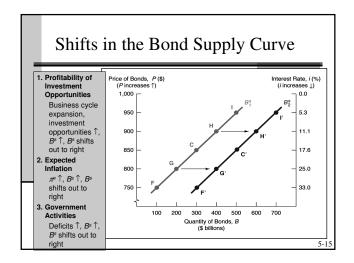
- Risk
  - risk of bonds $\Psi$ ,  $B^d \uparrow$ ,  $B^d$  shifts out to right
  - risk of other assets  $\uparrow$ ,  $B^d \uparrow$ ,  $B^d$  shifts out to right
- Liquidity
  - liquidity of bonds  $\uparrow$ ,  $B^d \uparrow$ ,  $B^d$  shifts out to right
  - liquidity of other assets  $\Psi$ ,  $B^d \uparrow$ ,  $B^d$  shifts out to right

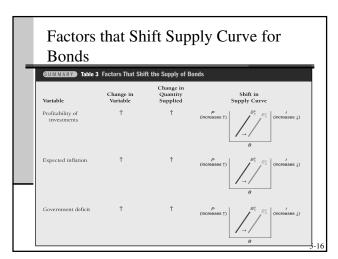
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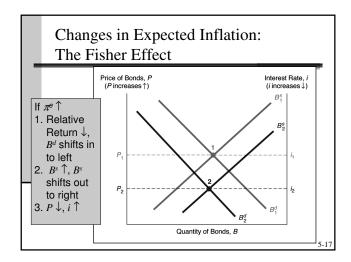
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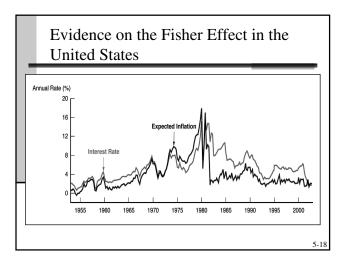


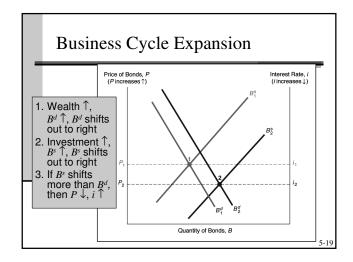


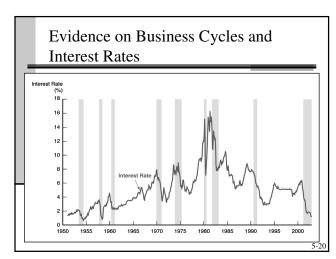












# Liquidity Preference Framework (Keynes)

- main assumption: two kinds of assets in the economy: money (i.e., currency) and bonds
- thus

 $M^s + B^s = Wealth$ 

- the budget constraint of the economy is:  $M^d + B^d = Wealth$
- therefore,  $M^s + B^s = M^d + B^d$
- rearranging the terms, we have that:  $M^s M^d = B^d B^s$
- the money market equilibrium occurs when M<sup>s</sup> = M<sup>d</sup>, which means that B<sup>s</sup> = B<sup>d</sup> and the bond market is in equilibrium as well

Relation to Loanable Funds Framework

- equating the supply and demand for bonds as in the loanable funds framework is equivalent to equating the supply and demand for money as in the liquidity preference framework
- the two frameworks are closely linked, but differ in practice because the liquidity preference assumes only two assets, money and bonds, and ignores the effects on interest rates from changes in expected returns on real assets

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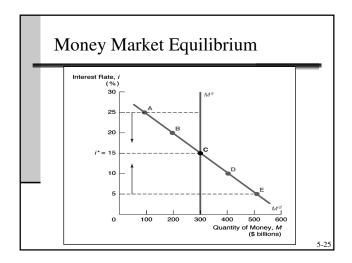
## Liquidity Preference Analysis

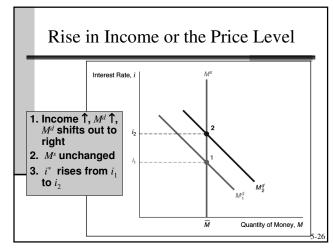
- Derivation of the money demand curve
  - Keynes assumed money bears zero interest
  - as  $i \uparrow$ , relative return on money  $\psi$  (equivalently, the opportunity cost of money  $\uparrow$ ), so demand for money  $\psi$
  - $\blacksquare$  so, the  $M^d$  curve has the usual downward slope
- Derivation of the money supply curve
  - lacktriangle we assume that the central bank controls the money supply  $M^s$  and it is a fixed amount
  - lacktriangle hence, the  $M^d$  curve is a vertical line

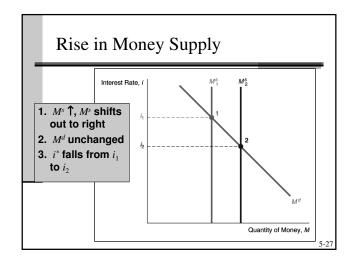
### Liquidity Preference Analysis (cont.)

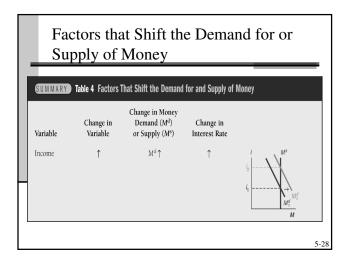
- Market equilibrium
  - lacktriangle occurs when money demand equals money supply,  $M^d = M^s$
  - suppose that, at the equilibrium,  $i^* = 15\%$
  - if i = 25%,  $M^s > M^d$  (excess supply): the price of bonds  $\uparrow$ ,  $i \lor$  to  $i^* = 15\%$
  - if i = 5%,  $M^d > M^s$  (excess demand): the price of bonds  $\Psi$ ,  $i \uparrow$  to  $i^* = 15\%$

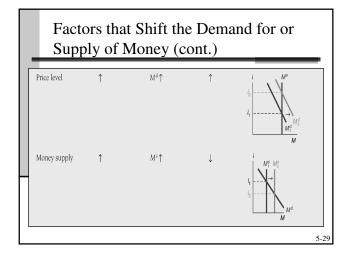
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## Effects of Money on Interest Rates

- liquidity effect:  $M^s \uparrow$ ,  $M^s$  shifts right,  $i \lor$
- *income effect*:  $M^s \uparrow$ , Income  $\uparrow$ ,  $M^d \uparrow$ ,  $M^d$  shifts right,  $i \uparrow$
- price level effect:  $M^s op$ , Price level op,  $M^d op$ ,  $M^d$  shifts right, i op
- expected inflation effect:  $M^s \uparrow$ ,  $\pi e \uparrow$ ,  $B^d \lor$ ,  $B^s \uparrow$ , Fisher effect,  $i \uparrow$
- hence, total effect of a change in money supply on interest rates is ambiguous because the income, price level and expected inflation effects work in the opposite direction of the liquidity effect

